

SURFACE AND VOLUME CURRENT IN A WIRE

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Reference: Griffiths, David J. (2007) Introduction to Electrodynamics, 3rd Edition; Prentice Hall - Problem 5.5.

A couple of examples of surface and volume current.

If we have a wire of radius a which carries a current I , what is the surface current K if the current in the wire is spread uniformly over the surface of the wire?

Since K is defined as the charge per unit width per unit time, we need the width over which the surface current is spread. This is just the circumference of the wire, so

$$(0.1) \quad K = \frac{I}{2\pi a}$$

Now suppose the current is distributed in the volume of the wire such that volume current density is inversely proportional to the distance from the axis. That is,

$$(0.2) \quad J = \frac{A}{r}$$

for some constant A . We need the total flow across the cross-sectional area of the wire to be the total current I , so we must have, using cylindrical coordinates:

$$(0.3) \quad I = \int_0^a \int_0^{2\pi} J d\phi r dr$$

$$(0.4) \quad = 2\pi A a$$

$$(0.5) \quad A = \frac{I}{2\pi a}$$

Thus the volume current density is

$$(0.6) \quad J = \frac{I}{2\pi ar}$$