

## BOUNDARY BETWEEN MAGNETIC MATERIALS

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References: Griffiths, David J. (2007) Introduction to Electrodynamics, 3rd Edition; Prentice Hall - Problem 6.26.

Just as electric field lines bend when crossing a boundary between two different dielectrics, so magnetic field lines bend when crossing a boundary between different permeabilities.

From the boundary conditions on the field  $\mathbf{B}$  and on the auxiliary field  $\mathbf{H}$  we have

$$(1) \quad B_{\perp}^{above} = B_{\perp}^{below}$$
$$(2) \quad \mathbf{H}_{\parallel}^{above} - \mathbf{H}_{\parallel}^{below} = \mathbf{K}_f \times \hat{\mathbf{n}}$$

If there is no free current at the boundary, then  $\mathbf{K}_f = 0$  and  $\mathbf{H}_{\parallel}^{above} = \mathbf{H}_{\parallel}^{below}$ . From the definition of permeability, we also have, for linear materials:

$$(3) \quad \mathbf{B} = \mu \mathbf{H}$$

If  $\theta_i$  is the angle between the normal to the boundary and the field lines  $\mathbf{B}_i$  in material  $i$ , then the conditions above come out to

$$(4) \quad B_1 \cos \theta_1 = B_2 \cos \theta_2$$

$$(5) \quad \frac{B_1 \sin \theta_1}{\mu_1} = \frac{B_2 \sin \theta_2}{\mu_2}$$

Dividing these two equations, we get

$$(6) \quad \frac{\tan \theta_1}{\tan \theta_2} = \frac{\mu_1}{\mu_2}$$

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