

## LORENTZ TRANSFORMATIONS AND SIMULTANEITY

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References: Griffiths, David J. (2007), Introduction to Electrodynamics, 3rd Edition; Pearson Education - Chapter 12, Post 13.

Here's a simple example of using the Lorentz transformations. Suppose that two events occur simultaneously in the Earth frame, a distance 500 km apart. An observer in a (very fast) plane travelling at  $\frac{12}{13}c$  along the line joining the events passes the first event  $A$  such that their respective coordinate origins coincide at that event. At what time does the plane observer think event  $B$  occurs?

The Lorentz transformations are

$$(1) \quad \bar{x} = \gamma(x - vt)$$

$$(2) \quad \bar{t} = \gamma\left(t - \frac{xv}{c^2}\right)$$

Event  $A$  occurs at the same time  $t = \bar{t} = 0$  in both systems. For event  $B$ ,  $x = 500$  km and  $t = 0$ , so

$$(3) \quad \bar{t} = \gamma\left(-\frac{500v}{c^2}\right)$$

$$(4) \quad \gamma = \frac{13}{5}$$

$$(5) \quad \bar{t} = -\frac{13}{5} \left(\frac{12c \ 500}{13 \ c^2}\right)$$

$$(6) \quad = -\frac{1200}{c}$$

$$(7) \quad = -\frac{1200 \text{ km}}{3 \times 10^5 \text{ km s}^{-1}}$$

$$(8) \quad = -4 \times 10^{-3} \text{ s}$$

Thus the plane observer thinks that  $B$  occurs 4 milliseconds before  $A$ .